

A cleared lunar distance is used to determine what GMT that distance corresponds to. The *Nautical Almanac* listed the lunar distances for the moon and various objects at three-hour intervals. The cleared distance would lie within one of those intervals.

The basic idea is to use interpolation to find the time corresponding to the cleared distance.

If

D is the angular difference between the tabulated distances that bracket your cleared distance ($dd^{\circ}mm'ss''_{UTC_i}$ and $dd^{\circ}mm'ss''_{UTC_{i+3}}$), its value to be used in calculations is given in the **P.L.** column of the *Precomputed Lunar Distances* table on the line of the first bracket ($dd^{\circ}mm'ss''_{UTC_i}$) in the form discussed below;

and

d is the angular difference between the earlier tabulated distance and your cleared distance: $dd^{\circ}mm'ss''_{UTC_i}$ and $dd^{\circ}mm'ss''_{UTC_{i+t}}$;

and

t is the yet unknown time interval hh:mm:ss between the earlier tabulated distance UTC and the moment of your lunar sight: UTC_i and UTC_{i+t} ;

then:

$$\frac{D}{d} = \frac{3 \text{ [hours]}}{t}$$

or,

$$t \text{ [hours]} = 3 \text{ [hours]} \cdot \frac{d}{D}$$

or,

$$t \text{ [seconds]} = 10800 \text{ [seconds]} \cdot \frac{d}{D}$$

To simplify this calculation the "*proportional logarithm*" of time **t** as being the common log of 10800 [seconds] minus the common log of **t** [seconds] was introduced in the *Tables Requisite*.

Because

$$D \cdot t = 10800 \cdot d$$

we can write:

$$\log D + \log t = \log 10800 + \log d$$

or,

$$\log t = \log 10800 + \log d - \log D$$

or, (subtracting each term from log of 10800 [seconds]):

$$\begin{aligned} (\log 10800 - \log t) &= \\ &= (\log 10800 - \log 10800) + (\log 10800 - \log d) - (\log 10800 - \log D) \end{aligned}$$

or,

$$(\log 10800 - \log t) = (\log 10800 - \log d) - (\log 10800 - \log D)$$

Therefore:

$$plog t = plog d - plog D$$

where *plog* is the *proportional logarithm* as defined above.

An example:

On 2015-Jan-01 the cleared distance between the Moon and Jupiter was found to be equal to 83°.

Looking up the *Precomputed Lunar Distances* table for that date one finds that the angle (83°) fits within the following brackets:

12:00 UT, 84° 35'.2, P.L. 2620
15:00 UT, 82° 56'.8, P.L. 2628

D, the total change in the distance during the three-hour interval (the angle between the brackets), equals to

$$84^\circ 35.2' - 82^\circ 56.8' = 1^\circ 38.4'$$

The value to be used in the calculations (2620) is given in the **P.L.** column of the *Precomputed Lunar Distances* table for first (12:00 UT) bracket, so:

$$\text{plog } \mathbf{D} = \underline{2620}$$

d is the angular difference between the distance tabulated for 12:00 UT and the distance cleared for the yet unknown time of lunar sight:

$$\mathbf{d} = 84^\circ 35.2' - 83^\circ 00.0' = 1^\circ 35.2'$$

Entering the ^h, ^m, column of the *Tables Requisite* with 1° 35.2' we find its' proportional logarithm value (2766) in the **P.L.** column, so:

$$\text{plog } \mathbf{d} = \underline{2766}$$

The plog **t** is:

$$\text{plog } \mathbf{t} = \text{plog } \mathbf{d} - \text{plog } \mathbf{D} = 2766 - 2620 = \underline{146}$$

Looking up 146 in *Tables Requisite* in the **P.L.** column we notice that it falls between the tabulated values of 145 and 147, which correspond to 2^h 54.1^m and 2^h 54.0^m or 02:54:06 and 02:54:00 respectively. The interpolated value of **t** is approximately equal to 02:54:03.

Adding the time offset **t** of the lunar to the UTC of the first tabulated bracket gives the UTC of the lunar sight itself:

$$12:00:00 + 02:54:03 = \underline{\mathbf{14:54:03}}$$