

```

#include "complexRobinStuart.h"

void main()
{
    {
        double GHA1 = DMS2D(6.0, 45.0, 58.06)*15.0;
        double Dec1 = -DMS2D(7.0, 51.0, 30.3);
        double HO1 = 90.0-DMS2D(61.0, 57.0, 30.0);
        double GHA2 = DMS2D(9.0, 49.0, 11.41)*15.0;
        double Dec2 = -DMS2D(7.0, 48.0, 37.3);
        double HO2 = 90.0-DMS2D(56.0, 34.0, 20.0);

        double B1, L1, B2, L2;

        char Bhms[50], Lhms[50];

        printf( "CoP1 = %lf\t%lf\t%lf\n", GHA1, Dec1, HO1 );
        printf( "CoP2 = %lf\t%lf\t%lf\n", GHA2, Dec2, HO2 );
        printf( "\n" );

        ComplexSolutionForIntersectionOfTwoCoP( GHA1, Dec1, HO1, GHA2, Dec2, HO2,
            &B1, &L1, &B2, &L2 );

        H2HMS( B1, Bhms );
        H2HMS( L1, Lhms );
        printf( "I1 = %lf, %lf = %s, %s\n", B1, L1, Bhms, Lhms );
        H2HMS( B2, Bhms );
        H2HMS( L2, Lhms );
        printf( "I2 = %lf, %lf = %s, %s\n", B2, L2, Bhms, Lhms );
        printf( "\n" );
    }
    {
        double GHA = DMS2D( 62, 16, 0 );
        double Dec = DMS2D( 38, 40, 13 );
        double B = DMS2D( 35, 30, 0 );
        double L = -DMS2D( 9, 30, 0 );
        double Hc, Z;
        char hms[50];

        ComplexSolutionForAltitudeAzimuth( GHA, Dec, B, L, &Hc, &Z );

        printf( "%lf\t%lf\t%lf\t%lf\n", GHA, Dec, B, L );
        H2HMS( Hc, hms );
        printf( "Hc = %lf = %s\n", Hc, hms );
        H2HMS( Z, hms );
        printf( "Z = %lf = %s\n", Z, hms );
        printf( "\n" );
    }
    {
        double dap = DMS2D( 103, 26, 24 );
        double HapM = DMS2D( 35, 37, 28 );
        double HapB = DMS2D( 40, 17, 24 );
        double HoM = DMS2D( 36, 26, 1 );
        double HoB = DMS2D( 40, 16, 15 );
        double theta = 0;
        double LD = 0;
        char hms[50];

        ComplexSolutionForClearingLunarDistance( dap, HapM, HapB, HoM, HoB, &theta, &LD );

        H2HMS( LD, hms );
        printf( "LD = %lf = %s\n", LD, hms );
        printf( "\n" );
    }
}

```

```
/*  
FILE: complexRobinStuart.c  
  
FUENTE: Applications of Complex Analysis to Celestial Navigation  
Robin G. Stuart  
Valhalla, New York, USA  
  
STATUS: Finalizado  
  
TEST: OK  
  
PENDIENTE: Hc/Z y LD  
  
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Andrés Ruiz. San Sebastian - Donostia. Gipuzkoa  
Navigational Algorithms  
Copyright (c) 2009  
*/  
  
#include "../Matematicas/angulos.h"  
  
double ModulusC( double a, double b )  
{  
    return( sqrt( a*a+b*b ) );  
}  
  
void ProductC( double r1, double i1, double r2, double i2, double *rp, double *ip )  
{  
    *rp = r1*r2-i1*i2;  
    *ip = r1*i2+r2*i1;  
}  
  
void InversoC( double a, double b, double *invR, double *invI )  
{  
    double k = SQ( ModulusC( a, b ) );  
    *invR = a/k;  
    *invI = -b/k;  
}  
  
void DivisionC( double r1, double i1, double r2, double i2, double *rp, double *ip )  
{  
    double invR, invI;  
    InversoC( r2, i2, &invR, &invI );  
    ProductC( r1, i1, invR, invI, rp, ip );  
}  
  
void Rec2Polar( double a, double b, double *r, double *fi )  
{  
    *r = sqrt( a*a+b*b );  
    *fi = ATAN2( b,a );  
}  
  
void Polar2Rec( double r, double fi, double *a, double *b )  
{  
    *a = r*COS(fi);  
    *b = r*SIN(fi);  
}  
  
void Euler( double fi, double *real, double *imag )  
{  
    *real = COS(fi);  
    *imag = SIN(fi);  
}  
  
void Zp( double Dec, double GHA, double *real, double *imaginary )  
{  
    double r = TAN( 45.0+Dec/2.0 );  
    Euler( -GHA, real, imaginary );  
  
    *real *= r;  
    *imaginary *= r ;  
}  
  
double Ro( double zd )
```

```

{
    return( TAN(zd/2.0) );
}

void Zc( double zpR,double zpI, double ro, double *real, double *imaginary )
{
    double mzp = ModulusC( zpR, zpI );
    double k = (1.0+ro*ro)/(1.0-ro*ro*mzp*mzp);
    *real = k*zpR;
    *imaginary = k*zpI ;
}

double Radius( double zpR,double zpI, double ro )
{
    double mzp = ModulusC( zpR, zpI );
    return( (1.0+mzp*mzp)/(1.0-ro*ro*mzp*mzp)*ro );
}

void ComplexSolutionForIntersectionOfTwoCoP( double GHA1, double Dec1, double Ho1,
                                             double GHA2, double Dec2, double Ho2,
                                             double* B1, double* L1,
                                             double* B2, double* L2 )
{
    double zp1R, zp1I;
    double zp2R, zp2I;
    double zc1R, zc1I;
    double r1;
    double zc2R, zc2I;
    double r2;

    double d;
    double mu, nu;
    double z1R, z1I;
    double z2R, z2I;

    double ZD1 = 90.0-Ho1;
    double ZD2 = 90.0-Ho2;

    Zp( Dec1, GHA1, &zp1R, &zp1I );
    Zc( zp1R, zp1I, Ro( ZD1 ), &zc1R, &zc1I );
    r1 = Radius( zp1R, zp1I, Ro( ZD1 ) );

    Zp( Dec2, GHA2, &zp2R, &zp2I );
    Zc( zp2R, zp2I, Ro( ZD2 ), &zc2R, &zc2I );
    r2 = Radius( zp2R, zp2I, Ro( ZD2 ) );

    d = ModulusC( zc1R-zc2R, zc1I-zc2I );
    mu = (SQ(r1)-SQ(r2))/(2.0*SQ(d));
    nu = 1.0/(2.0*SQ(d))*sqrt( 4.0*SQ(r1)*SQ(d)-SQ(SQ(d)+SQ(r1)-SQ(r2)) );

    { // Intersection of the 2 CoP on the complex plane
    double pR, pI;

    ProductC( mu, nu, zc2R-zc1R, zc2I-zc1I, &pR, &pI );
    z1R = 1.0/2.0*(zc1R+zc2R)+pR;
    z1I = 1.0/2.0*(zc1I+zc2I)+pI;

    ProductC( mu, -nu, zc2R-zc1R, zc2I-zc1I, &pR, &pI );
    z2R = 1.0/2.0*(zc1R+zc2R)+pR;
    z2I = 1.0/2.0*(zc1I+zc2I)+pI;
    }

    { // Intersection of the 2 CoP in (B,L)
    double r1, fi1;
    Rec2Polar( z1R, z1I, &r1, &fi1 );

    *B1 = 2.0*(ATAN(r1)-45.0);
    *L1 = fi1;
    }
    {
    double r2, fi2;
    Rec2Polar( z2R, z2I, &r2, &fi2 );

    *B2 = 2.0*(ATAN(r2)-45.0);
    *L2 = fi2;
    }

    printf( "Zp1 = (%lf, %lf i)\n", zp1R, zp1I );
    printf( "ro1 = %lf\n", Ro( ZD1 ) );
    printf( "Zc1 = (%lf, %lf i)\n", zc1R, zc1I );
    printf( "r1 = %lf\n", r1 );
    printf( "\n" );
}

```

```

printf( "Zp2 = (%lf, %lf i)\n", zp2R, zp2I );
printf( "ro2 = %lf\n", Ro( ZD2 ) );
printf( "Zc2 = (%lf, %lf i)\n", zc2R, zc2I );
printf( "r2 = %lf\n", r2 );
printf( "\n" );

printf( "d = %lf\n", d );
printf( "mu = %lf\n", mu );
printf( "nu = %lf\n", nu );

printf( "Z1 = (%lf, %lf i)\n", z1R, z1I );
printf( "Z2 = (%lf, %lf i)\n", z2R, z2I );
printf( "\n" );
}

void ComplexSolutionForAltitudeAzimuth( double GHA, double Dec, double B, double L, double* Hc, double* Z )
{
    double aR, aI;
    double bR, bI, mb;
    double zR, zI;
    double wR, wI;

    double nR, nI, dR, dI;

    Euler( -L/2.0, &aR, &aI );

    mb = TAN( 45.0+B/2.0 );
    Euler( L/2.0+180.0, &bR, &bI );
    bR *= mb;
    bI *= mb;

    Zp( Dec, GHA, &zR, &zI );

    // T(z)
    ProductC( aR, aI, zR, zI, &nR, &nI );
    nR += bR;
    nI += bI;

    ProductC( -bR, bI, zR, zI, &dR, &dI );
    dR += aR;
    dI -= aI;

    DivisionC( nR, nI, dR, dI, &wR, &wI );

    {
        double r, fi;
        Rec2Polar( wR, wI, &r, &fi );

        *Hc = 2.0*(45.0-ATAN(r));
        *Z = fi;

        printf( "w = (%lf, %lf i) = %lf e %lf i\n", wR, wI, r, DegRad(fi) );
    }

    // Hemisferio S (1.2)
    //kk

    printf( "a = (%lf, %lf i)\n", aR, aI );
    printf( "b = (%lf, %lf i)\n", bR, bI );
    printf( "mb = %lf\n", mb );
    printf( "z = (%lf, %lf i)\n", zR, zI );
    printf( "w = (%lf, %lf i)\n", wR, wI );
    printf( "\n" );
}

double ComplexLunarDistance( double z1, double z2, double theta )
{
    double d;

    d = 2.0*ATAN( sqrt( (z1*z1+z2*z2-2.0*z1*z2*COS(theta))/(1.0+z1*z1*z2*z2+2.0*z1*z2*COS(theta)) ) );

    return( d );
}

double ComplexAzimuthDifference( double z1, double z2, double d )
{
    double theta;

    theta = ACOS( (SQ(z1)+SQ(z2)-(1.0+SQ(z1)*SQ(z2))*SQ(TAN(d/2.0)))/(2.0*z1*z2*(1.0+SQ(TAN(d/2.0)))) );

    return( theta );
}

```

```
double Z_H( double H )
{
    printf( "z = %lf\n", TAN( 45.0-H/2.0 ) );
    return( TAN( 45.0-H/2.0 ) );
}

void ComplexSolutionForClearingLunarDistance( double dap, double HapM, double HapB, double HoM, double HoB,
double* theta, double* LD )
{
    double cm = 0; // dip, R, PA, AG, ...
    double cb = 0;
    double z1 = Z_H( HapM+cm );
    double z2 = Z_H( HapB+cb );

    double z1o = Z_H( HoM );
    double z2o = Z_H( HoB );

    *theta = ComplexAzimuthDifference( z1, z2, dap );

    *LD = ComplexLunarDistance( z1o, z2o, *theta );
}
```